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Resource-rational decision making Rahul Bhui¹, Lucy Lai² and Samuel J Gershman^{3,4}



Across many domains of decision making, people seem both rational and irrational. We review recent work that aims to reconcile these apparently contradictory views by modeling human decisions as optimal under a set of cognitive resource constraints. This 'resource-rational' analysis connects psychology and neuroscience to ideas from engineering, economics, and machine learning. Here, we focus on an information-theoretic formalization of cognitive resources, highlighting its implications for understanding three important and widespread phenomena: reference dependence, stochastic choice, and perseveration. While these phenomena have traditionally been viewed as irrational biases or errors, we suggest that they may arise from a rational solution to the problem of resource-limited decision making.

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Introduction

A paradox resides at the heart of behavioral science. Much work focuses on the complex tasks that people successfully solve in domains ranging from sensory perception to social communication [1–7]; yet, an equally important body of research lists our seemingly countless deviations from optimality, often at the same time [8–10]. How might one explain the 'apparent contradictions between the great triumphs and the dramatic failures of the human mind' [11]?

Here, we review recent work that seeks to resolve this paradox by formalizing the idea that people are doing as best as they can subject to constraints on cognitive resources. This resource-rational (or computationally rational) perspective [12–14,15**] lets us rigorously capture both the method and the madness of human judgment in the same thrust — that is, the adaptive logic behind decision making as well as its systematic limitations. The world is vast, but we have only limited cognitive capacities with which to grasp it. We are thus forced to mentally represent information about the world as economically as possible. We take shortcuts by compressing or distorting or flat-out ignoring parts of the world — at least, when we can get away with it. Models of resource rationality clarify which corners are worth cutting and how we should cut them.

Resource rationality refines traditional views of bounded rationality by conceiving of judgment as optimal under cognitive costs or constraints, rather than merely feasible. By casting mental processes in the mathematics of optimization, this approach enables precise descriptions of how we deploy limited cognitive resources where they are most valuable, and lets us trace out how decision making is shaped as a result. To achieve this blend of tractability and realism, resource-rational analysis links psychology and neuroscience with concepts from engineering, economics, information theory, statistics, and machine learning. In this article, we focus on analyses using information theory, which offers a versatile mathematical language for defining efficiency. Below, we outline some examples of important behavioral phenomena that this approach has helped to characterize.

Reference dependence and efficient coding

Abundant research [23] and personal experience tell us that our feelings about an outcome depend on how we compare it to our other experiences. However, exactly what kinds of comparisons do we make? And for that matter, why do we even make comparisons at all? Answers lie in the *principle of efficient coding* [24,25], which asserts that brains represent information in a cost-effective manner by adapting our neural representations to the local statistics of our environment. While an idealized agent would be able to perfectly assign values to all possible outcomes and have completely rational preferences, real humans cannot be sensitive to the entire spectrum of conceivable values at the same time. To operate within this limitation, the brain must preferentially dedicate its resources to representing the most likely stimulus values [26].

To formalize a version of this idea, consider the problem of finding a mapping p(r|x) from a real-valued stimulus to an internal representation so as to maximize information transmission (Box 1), defined as the mutual information

Box 1 Formalizing efficiency

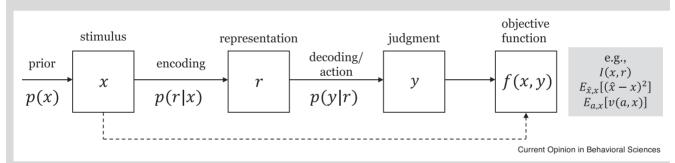
Perceptual and cognitive processes can be described as the transmission of information through a communication channel with limited capacity, illustrated in Figure I. A stimulus (x with prior distribution p(x)) must be encoded in an internal representation (r given by the encoder p(r|x)) which can only imperfectly represent the stimulus. A judgment is formed, which could reflect a decoded reconstruction of the stimulus $(\hat{x} \text{ following } p(\hat{x}|r))$ or an action (a according to policy $p(a|\hat{x})$, yielding state-dependent reward value v(a,x)).

Efficiency obtains when some measure of the representation's fidelity (or consequent reward) is optimized given a cost or constraint on information transmission. Models are typically constructed by making assumptions about some aspects of this process and characterizing the rest based on what is optimal according to the objective function. Three classes of objective functions are commonly used in information-theoretic analyses:

- 1. Maximization of mutual information, $I(x,r) \equiv H(r) H(r|x)$ where $H(r) \equiv E[-\log p(r)]$ is the entropy [16] that expresses uncertainty about variable r, and H(r|x) is the conditional entropy that expresses uncertainty about r conditional on x. This criterion can be maximized exactly or via an approximation like Fisher information [17]. It can be interpreted as the reduction in uncertainty about r after observing x, or vice versa, because it is a symmetric measure.
- 2. Minimization of squared loss, $E_{\hat{x}}$, $x[(\hat{x}-x)^2]$. This criterion can be minimized subject to a cost or constraint on information capacity, often defined in terms of mutual information. It is often used in rate-distortion theory and economic analyses of capacity-limited decision making [18
- 3. Maximization of reward, $E_{ax}[v(a,x)]$. This criterion can be maximized subject to a cost or constraint on information capacity often defined in terms of mutual information. It explicitly captures the consequences of actions taken based on the representation.

These objective functions formalize constraints that are internal to an agent, but another impetus for efficiency comes from external constraints, namely the limited data available to the agent. Results in statistical learning theory show that in order to generalize, an agent must be able to compress its data [20,21]. This principle has motivated recent algorithms in machine learning, such as the variational autoencoder [22], that extract low complexity structure by pushing data through an information bottleneck, typically a low-dimensional layer in a deep neural network.

Figure I



A view of cognition as a communication channel

between the two, I(x,r). For simplicity, suppose the encoding process is deterministic, but the representation only comprises a limited number of internal states; we can think of it as a step function with output normalized to the unit interval. Since the set of internal states is coarser than the set of possible values, compression is required. When the number of internal states grows large, the optimal solution in this setting approaches the cumulative distribution function (CDF) of the stimulus distribution [27]:

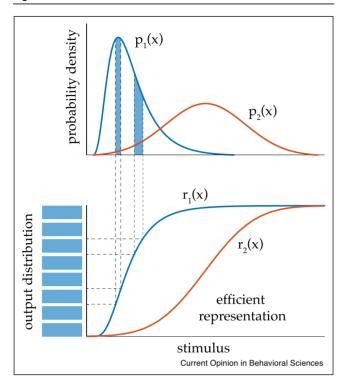
$$r^* = F(x) \equiv \int_{-\infty}^{x} p(x')dx'.$$

The same solution also results from minimizing the probability of making errors when ranking two values drawn from the prior distribution [28].

Observe that this representation is not fixed, but instead mirrors the context as defined by the environmental distribution of stimulus values. It is most sensitive to

variation within the most likely ranges of values, as the CDF is steep where the probability density function is high. For example, if values follow a bell-shaped prior (as illustrated in Figure 1), the representation is an S-shaped function, sensitive near the median but insensitive at the extremes. It shifts when the prior shifts and flattens when the prior flattens. This property reveals how preferences should be shaped by the entire contextual distribution, rather than only a single reference point as in standard models of reference dependence. Consistent with the efficient coding hypothesis, experiments have demonstrated that sensitivity to value differences between options tends to decrease: Firstly, when values are far away from the reference point (the prior mean), reflecting a form of diminishing sensitivity similar to Weber's law for magnitude discrimination [30,31]; and finally, when the variance of values across options is large [32]. Furthermore, the same value is judged as more or less attractive to the degree that it is higher or lower (respectively) than the reference point [33–35].

Figure 1



Context-dependent value function resulting from efficient coding. The optimal representation with a fixed output range is given by the CDF of the prior stimulus distribution. It is sensitive to gradations near the peak of the prior, where values are most frequently encountered, and insensitive at the tails, which are rarely experienced. As the prior changes, such as from p_1 to p_2 , so does the efficient representation, from r_1 to r_2 . Adapted from [29].

The CDF transformation is approximated by the psychological process model of decision by sampling [36,37,38°] which has been proposed to account for malleability in representations of economic attributes (like values, probabilities, and delays) beyond the reach of traditional models. The key idea is that when judging an attribute, a decision maker constructs a relativistic representation by sampling attribute magnitudes stored in memory and comparing these samples ordinally to the target attribute magnitude. If memory is assumed to reflect the ecological distribution of magnitudes, then we can understand the sampling and comparison process as a Monte Carlo approximation of the CDF. Importantly, this means that the encoding process is noisy and the optimal internal representation needs to compensate for this noise, which can be accomplished by kernel smoothing the samples [38°]. One consequence of this modification is that judgments will be sensitive not only to the rank of attribute magnitudes (via the CDF) but also to their range. A fixed number of samples spread across a wider range of magnitudes means that the attribute space is more sparsely sampled, and therefore needs a greater smoothing bandwidth to compensate for noise. This results in a form of range normalization: discriminability of magnitudes decreases with range. Many studies of judgment and decision making have provided evidence for range normalization in choice [39-41]. More specifically, the balance between rank and range effects may be predicted based on the optimal degree of smoothing for a given level of noise in the encoding process [38°].

Variations on this theme emerge when making alternative assumptions about the elements depicted in Box 1. For example, the stimulus might consist of multiple items or attributes; in this case, efficiency requires encoding to be based on combinations of these dimensions that increase the statistical independence of the representational components. This function may be implemented by divisive normalization, which could account for violations of classic axioms of rational choice [42–46]. Other objectives or constraints may also be considered [47,48,49°]; for instance, reward, rather than information capacity, might be taken as the criterion to maximize [50,51°,52]. While evidence for reference dependence is abundant in both brain [26,33] and behavior [23,53,54], these lines of theorizing could help pin down its nature more precisely by clarifying the conditions under which we should expect its different guises. Recent empirical evidence indicates that decision by sampling provides a better quantitative account of incentivized decision making compared to other models of efficient coding which maximize accuracy or reward, suggesting that it may be a particularly robust and pervasive cognitive process [51°].

The context dependence arising in these types of models recapitulates the influential idea of ecological rationality, according to which rationality emerges from the match between the cognitive strategy of the agent and the structure of its environment [55,56]. The same concept is plainly seen in the domain of sensory perception, where the principle of efficient coding originated; just as our eyes acclimate to light or dark and our ears get accustomed to noise or silence, our sense of value adapts to the level of rewards in our local environment. In fact, much of our understanding of context dependence in preferences stems from analogous research on perception [57], from the current era (e.g. [58-61,17,62]) back to the very inception of behavioral economics [30,63]. These deep interdisciplinary links underscore the unifying power of resource rationality.

Stochastic choice and perseveration

Even when faced with the same decision, our choices may vary in a random fashion [64]. This inconsistency can occur because the quality of judgment is limited by how precisely our brains represent values [65] (or states of the world which indicate values). While randomness in choice has often been treated as exogenously determined, an alternative perspective emerges from the idea that agents can control the richness of their representations. Higherfidelity representations let us cleanly distinguish between different states and make it clear which action is best, but are costlier to implement [66°]. Thus, there is a tradeoff between the complexity of the representation and the reward that the corresponding action policy achieves.

To formalize core elements of this *reward-complexity* tradeoff, consider the problem of finding a policy p(a|x) which maps states of the world to actions in order to maximize expected reward (Box 1). Critically, this mapping incurs a cost proportional to the complexity of the state representation, as measured by the mutual information between states and actions, I(a,x). The agent thus selects a policy to maximize $\beta E_{a,x}[v(a,x)] - I(a,x)$, where β reflects the added value of a 1-bit increase in the fidelity of the state representation. The optimal action policy that solves this trade-off is given by [67-72]

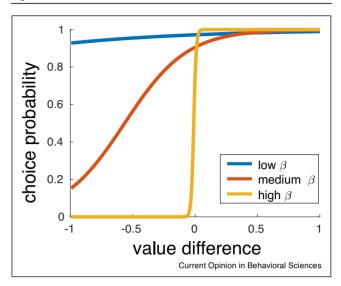
$$p^*(a|x) = \frac{\exp[\beta v(a,x) + \log p^*(a)]}{\sum_{a'} \exp[\beta v(a',x) + \log p^*(a')]},$$

where $p^*(a) = \sum_x p^*(a|x)p(x)$ is the marginal action distribution.

This policy has three key features, which can be seen in Figure 2. First, it takes the familiar form of the softmax function (also known as the multinomial logit model or the Boltzmann distribution). Note that this form results from the entropy-based cost function rather than from convenient assumptions about the shape of the noise distribution. Second, the inverse temperature parameter, which regulates the degree of choice stochasticity, is given by the β parameter which quantifies the benefit of a complex representation. When β is high, the policy will be concentrated on the best action in each state. Third, the bias term is interpretable as the marginal action distribution, $p^*(a)$, meaning that choices are biased toward actions that are frequently chosen across states. When it is not very beneficial to discern the best action (β is low), choices become less sensitive to payoffs of actions and more dependent on the marginal distribution.

This line of thinking can be extended to various dynamic settings. The above expression could summarize the choice probabilities resulting from a noisy process of deliberation taking place in real time [73,74]. Such findings help normatively ground and expand upon classic sequential sampling models that jointly capture choice stochasticity and response time. Or, if learning happens over multiple trials, a kind of perseveration occurs as choice probabilities appear to recapitulate one's prior action history [75,76]. Inertia can be adaptive when states are correlated across time, because learning about state transitions is costly, so the agent tends to rely on their prior experience and repeat their previous actions [77]. In complex multi-step tasks such as navigation, policy

Figure 2



Complexity-dependent binary choice probabilities. The focal option here tends to be better in more states of the world. When the benefit of a complex representation is high (or equivalently, the cost of information transmission is low), the agent almost deterministically selects whichever option is best in each situation (yellow line). When information is relatively costly, choice is stochastic with a bias toward the action which tends to be chosen more often across states (red line). As capacity becomes severely constrained, the bias dominates and the agent almost always selects the marginally high frequency action, ignoring the true state (blue line).

compression can yield a noisier version of the ideal trajectory or even an alternative path that is more tolerant of noise [68,78°]. Moreover, the coarsened representation reflects efficient state abstraction (e.g. clustering together locations in the same room) and subgoals naturally emerge at the transition from one state cluster (e.g. room) to the next [79,80].

In sum, we may endure randomness when it is not worth eliminating, and use strategies that compensate for its consequences. These strategies can manifest as biases or imperfections despite having adaptive value, like taking a longer, but simpler, route between two points in a city to avoid the risk of getting lost. Errors and biases can thus be two sides of the same coin. These kinds of mechanisms may shed light on properties of noisy and biased perceptions of value [48,51°] and probability [81–83], risky [84] and intertemporal choice [85], and a wide variety of other economic outcomes [19°°].

Conclusions

We have dipped our toes into the ocean of resource rationality [15°°], focusing on its implications for decision making. The idea that cognitive resources are spent when and where they are most needed can be flexibly specified and applied to a vast array of decision problems, illuminating a number of mental shortcuts. Different

disciplines vary in their willingness to trade off psychological realism for formal tractability [86]. Resource-rational analysis targets the middle ground and aims to expand the frontier of possibilities — to achieve a greater mix of realism and tractability than traditionally attainable.

Perhaps the deepest implication of the resource-rational approach is to help fundamentally change the way we treat apparently irrational behavior. Phenomena such as those discussed in this paper are often viewed as strange defects of the human mind, challenging our ability to systematically explain them. Resource-rational analysis provides us with a path forward that respects both the intelligent nature of our judgment and the constraints we face as real flesh and blood creatures. It is a unified lens through which to view the entirety of the mind, including key facets of judgment and decision making alongside core cognitive functions like perception, attention, and memory. And rather than treating biases and errors as bizarre quirks, oddities, or eccentricities of the mind, sometimes we find that they reflect sensible adaptations to cognitive limits, as sure as our eyes adapt to light and dark every day of our lives.

Conflict of interest statement

Nothing declared.

References and recommended reading

Papers of particular interest, published within the period of review, have been highlighted as:

- · of special interest
- of special interest
- Knill DC, Richards W: Perception as Bayesian Inference. Cambridge University Press; 1996.
- Todorov E: Optimality principles in sensorimotor control. Nat Neurosci 2004, 7:907-915.
- 3. Yuille A, Kersten D: Vision as Bayesian inference: analysis by synthesis? Trends Coan Sci 2006, 10:301-308.
- Griffiths TL, Tenenbaum JB: Optimal predictions in everyday cognition. Psychol Sci 2006, 17:767-773.
- Oaksford M, Chater N: Bayesian rationality the probabilistic approach to human reasoning. Oxford Cognitive Science Series.
- Bogacz R: Optimal decision-making theories: linking neurobiology with behaviour. Trends Cogn Sci 2007, 11:118-
- Frank MC, Goodman ND: Predicting pragmatic reasoning in language games. Science 2012, 336:998.
- Ariely D: Predictably Irrational: The Hidden Forces That Shape Our Decisions. 2008:280.
- Marcus G: Kluge: The Haphazard Evolution of the Human Mind. Houghton Mifflin Harcourt; 2009.
- 10. Kahneman D: Thinking, Fast and Slow. Macmillan; 2011.
- 11. Ross L, Nisbett RE: The person and the situation: Perspectives of social psychology. McGraw-Hill Series in Social Psychology. 1991-286
- 12. Lewis RL, Howes A, Singh S: Computational rationality: linking mechanism and behavior through bounded utility maximization. Top Cogn Sci 2014, 6:279-311.

- 13. Gershman SJ, Horvitz EJ, Tenenbaum JB: Computational rationality: a converging paradigm for intelligence in brains, minds, and machines. Science 2015, 349:273-278.
- 14. Griffiths TL, Lieder F, Goodman ND: Rational use of cognitive resources: levels of analysis between the computational and the algorithmic. Top Cogn Sci 2015, 7:217-229.
- 15. Lieder F. Griffiths TL: Resource-rational analysis:
- understanding human cognition as the optimal use of limited computational resources. Behav Brain Sci 2020. 43 This modern review of resource rationality discusses a wide variety of applications, accompanied by commentary from many scholars.
- 16. Cover TM, Thomas JA: Elements of Information Theory. John Wiley & Sons: 2006.
- 17. Wei X-X, Stocker AA: Mutual information, fisher information, and efficient coding. Neural Comput 2016, 28:305-326.
- Sims CA: Implications of rational inattention. J Monetary Econ. 2003. **50**:665-690.
- 19. Mackowiak B, Matejka F, Wiederholt M: Rational Inattention: A Review. Technical Report 15408. 2020
- This modern review provides a clear introduction to capacity-limited decision making, laying out its assumptions and implications in-depth and describing its applications to subfields of economics.
- 20. Blumer A, Ehrenfeucht A, Haussler D, Warmuth MK: Occam's razor. Inform Process Lett 1987, 24:377-380.
- 21. Blum A. Langford J: PAC-MDL bounds. Learning Theory and Kernel Machines. Springer; 2003:344-357.
- 22. Kingma DP, Welling M: Auto-encoding variational Bayes. The 2nd International Conference on Learning Representations 2013.
- 23. O'Donoghue T, Sprenger C: Reference-dependent preferences. Handbook of Behavioral Economics: Applications and Foundations 1. Elsevier; 2018:1-77.
- 24. Attneave F: Some informational aspects of visual perception. Psychol Rev 1954, 61:183-193.
- 25. Barlow HB: Possible principles underlying the transformation of sensory messages. Sens Commun 1961, 1:217-234.
- 26. Rangel A, Clithero JA: Value normalization in decision making: theory and evidence. Curr Opin Neurobiol 2012, 22:970-981
- 27. Laughlin S: A simple coding procedure enhances a neuron's information capacity. Zeit Naturforsch C 1981, 36:910-912
- 28. Robson AJ: The biological basis of economic behavior. J Econ Lit 2001, 39:11-33.
- 29. Wark B, Lundstrom BN, Fairhall A: Sensory adaptation. Curr Opin Neurobiol 2007, 17:423-429.
- 30. Kahneman D, Tversky A: Prospect theory: an analysis of decision under risk. Econometrica 1979, 47:263-292.
- 31. Erev I, Ert E, Yechiam E: Loss aversion, diminishing sensitivity, and the effect of experience on repeated decisions. J Behav Decis Making 2008, 21:575-597.
- 32. Rigoli F, Friston KJ, Martinelli C, Selaković M, Shergill SS, Dolan RJ: A Bayesian model of context-sensitive value attribution. ELife 2016, 5:e16127.
- 33. Rigoli F, Friston KJ, Dolan RJ: Neural processes mediating contextual influences on human choice behaviour. Nat Commun 2016, 7:1-11,
- 34. Simonsohn U, Loewenstein G: Mistake #37: The effect of previously encountered prices on current housing demand. Econ J 2006, 116:175-199.
- 35. Ungemach C, Stewart N, Reimers S: How incidental values from the environment affect decisions about money, risk, and delay. Psychol Sci 2011, 22:253-260.
- 36. Stewart N, Chater N, Brown GDA: Decision by sampling. Cogn Psychol 2006, 53:1-26.

- Mullett TL, Tunney RJ: Value representations by rank order in a distributed network of varying context dependency. Brain Cogn 2013, 82:76-83.
- Bhui R, Gershman SJ: Decision by sampling implements
 efficient coding of psychoeconomic functions. Psychol Rev 2018, 125:985-1001

This theoretical article reveals how classic, influential models of contextsensitive economic judgment based on rank and range normalization can be derived from an efficient coding analysis.

- Parducci A: Happiness, Pleasure, and Judgment: The Contextual Theory and Its Applications. 1995.
- Soltani A, De Martino B, Camerer C: A range-normalization model of context-dependent choice: a new model and evidence. PLoS Comput Biol 2012, 8:e1002607.
- Rustichini A, Conen KE, Cai X, Padoa-Schioppa C: Optimal coding and neuronal adaptation in economic decisions. Nat Commun 2017. 8:1-14.
- **42.** Louie K, Grattan LE, Glimcher PW: **Reward value-based gain control: divisive normalization in parietal cortex**. *J Neurosci* 2011, **31**:10627-10639.
- **43.** Louie K, Khaw MW, Glimcher PW: **Normalization is a general neural mechanism for context-dependent decision making.** *Proc Natl Acad Sci U S A* **2013, 110**:6139-6144.
- Khaw MW, Glimcher PW, Louie Ky: Normalized value coding explains dynamic adaptation in the human valuation process. Proc Natl Acad Sci U S A 2017, 114:12696-12701.
- Steverson K, Brandenburger A, Glimcher P: Choice-theoretic foundations of the divisive normalization model. J Econ Behav Organ 2019, 164:148-165.
- Webb R, Glimcher PW, Louie K: The normalization of consumer valuations: context-dependent preferences from neurobiological constraints. Manag Sci 2020.
- Rayo L, Becker GS: Evolutionary efficiency and happiness. J Polit Econ 2007, 115:302-337.
- 48. Woodford M: Prospect theory as efficient perceptual distortion. Am Econ Rev 2012, 102:41-46.
- 49. Polanía R, Woodford M, Ruff CC: Efficient coding of subjective
 value. Nat Neurosci 2019, 22:134-142

This study finds that a theory of efficient coding and Bayesian decoding previously applied to perception can account for intricate patterns of bias in representations of value.

- Netzer N: Evolution of time preferences and attitudes toward risk. Am Econ Rev 2009, 99:937-955.
- 51. Heng JA, Woodford M, Polania R: Efficient sampling and noisydecisions. Elife 2020:9

This study develops models of efficient coding that maximize accuracy and reward in a numerosity discrimination task, and compares their empirical performance to decision by sampling, which fits the data better.

- Juechems K, Balaguer J, Spitzer B, Summerfield C: Optimal Utility and Probability Functions for Agents With Finite Computational Precision. 2020.
- Bavard S, Lebreton M, Khamassi M, Coricelli G, Palminteri S: Reference-point centering and range-adaptation enhance human reinforcement learning at the cost of irrational preferences. Nat Commun 2018, 9:1-12.
- Rigoli F: Reference effects on decision-making elicited by previous rewards. Cognition 2019, 192:104034.
- Simon HA: Rational choice and the structure of the environment. Psychol Rev 1956, 63:129.
- Todd PM, Gigerenzer G: Bounding rationality to the world. J Econ Psychol 2003, 24:143-165.
- Louie K, Glimcher PW: Efficient coding and the neural representation of value. Ann N Y Acad Sci 2012, 1251:13-32.
- Carandini M, Heeger DJ: Normalization as a canonical neural computation. Nat Rev Neurosci 2012, 13:51-62.

- Lyu S, S EP: Nonlinear extraction of independent components of natural images using radial gaussianization. Neural Comput 2009. 21:1485-1519.
- Lyu S: Dependency reduction with divisive normalization: justification and effectiveness. Neural Comput 2011, 23:2942-2973
- 61. Wei X-X, Stocker AA: Efficient coding provides a direct link between prior and likelihood in perceptual bayesian inference. In Advances in Neural Information Processing Systems, , vol 25. Edited by Pereira F, Burges CJC, Bottou L, Weinberger KQ. Curran Associates, Inc; 2012:1304-1312.
- Wei X-X, Stocker AA: Lawful relation between perceptual bias and discriminability. Proc Natl Acad Sci U S A 2017, 114:10244-10249.
- Kahneman D: Maps of bounded rationality: psychology for behavioral economics. Am Econ Rev 2003, 93:1449-1475.
- 64. Michael W: Modeling imprecision in perception, valuation, and choice. Annu Rev Econ 2020, 12:579-601.
- 65. Aldo Faisal A, Selen LPJ, Wolpert DM: Noise in the nervous system. *Nat Rev Neurosci* 2008, 9:292-303.
- Zenon A, Solopchuk O, Pezzulo G: An information-theoretic
 perspective on the costs of cognition. Neuropsychologia 2019, 123:5-18

This article elaborates on the connections between information costs and cognitive costs, translating between computational quantities and psychological content.

- Parush N, Tishby N, Bergman H: Dopaminergic balance between reward maximization and policy complexity. Front Syst Neurosci 2011, 5:22.
- 68. Tishby N, Polani D: *Information Theory of Decisions and Actions*.
- Still S, Precup D: An information-theoretic approach to curiosity-driven reinforcement learning. Theory Biosci 2012, 131:139-148.
- Caplin A, Dean M: Behavioral Implications of Rational Inattention With Shannon Entropy. Technical Report. National Bureau of Economic Research; 2013.
- Ortega PA, Braun DA: Thermodynamics as a theory of decision-making with information-processing costs. Proc R Soc A: Math Phys Eng Sci 2013, 469:2020683.
- Matějka F, McKay A: Rational inattention to discrete choices: a new foundation for the multinomial logit model. Am Econ Rev 2015, 105:272-298.
- Hébert BM, Woodford M: Rational Inattention When Decisions Take Time. Technical Report. National Bureau of Economic Research; 2019.
- 74. Zhong W: Optimal Dynamic Information Acquisition. 2019.
- Gershman SJ: Origin of perseveration in the trade-off between reward and complexity. Cognition 2020, 204:104394.
- Gershman SJ, Lai L: The reward-complexity trade-off in schizophrenia. bioRxiv 2020.
- Steiner J, Stewart C, Matějka F: Rational inattention dynamics: inertia and delay in decision-making. Econometrica 2017, 85:521-553.
- Rubin J, Shamir O, Tishby N: Trading value and information in mdps. Decision Making with Imperfect Decision Makers. Springer; 2012:57-74

This piece characterizes a capacity-constrained version of reinforcement learning which the authors apply to navigation, demonstrating how efficient action policies are stochastic and may be altered to compensate for this stochasticity.

 Van Dijk SG, Polani D: Informational constraints-driven organization in goal-directed behavior. Adv Complex Syst 2013, 16:1350016.

- 80. Botvinick M, Weinstein A, Solway A, Barto A: Reinforcement learning, efficient coding, and the statistics of natural tasks. Curr Opin Behav Sci 2015, 5:71-77.
- 81. Steiner J, Stewart C: Perceiving prospects properly. Am Econ Rev 2016, 106:1601-1631.
- 82. Gossner O, Steiner J: On the cost of misperception: general results and behavioral applications. *J Econ Theory* 2018, **177**:816-847.
- 83. Dasgupta I, Schulz E, Tenenbaum JB, Gershman SJ: A theory of learning to infer. Psychol Rev 2020, 127:412.
- 84. Frydman C, Jin LJ: Efficient Coding and Risky Choice. 2020.
- 85. Gershman SJ, Bhui R: Rationally inattentive intertemporal choice. Nat Commun 2020, 11:3365.
- 86. Rabin M: A perspective on psychology and economics. Eur Econ Rev 2002, 46:657-685.